

## 11.5: Case-Control Studies

### Independent samples

	D+	D-	Total
E+	$A_1$	$B_1$	$N_1$
E-	$A_0$	$B_0$	$N_2$
Total	$M_1$	$M_0$	$N$

- The **odds ratio**  $\hat{OR} = \frac{A_1 B_0}{A_0 B_1}$ . (The second edition of the text uses this symbol  $\hat{\psi}$  to represent the odds ratio estimate.
- The odds ratio in the population is stochastically equivalent to its rate ratio. When risks in the population are low (less than 5%), the odds ratio may be interpreted as a risk ratio.
- The standard error of natural log (ln) of the odds ratio is  $SE = \sqrt{\frac{1}{A_1} + \frac{1}{B_1} + \frac{1}{A_0} + \frac{1}{B_0}}$ . A 95% confidence interval for the *OR* parameter is given by  $e^{\ln \hat{OR} \pm (1.96)(SE)}$ .
- A *P* value can be derived with this test statistic: 
$$z = \frac{A_1 - \frac{N_1 M_1}{N}}{\sqrt{\frac{N_1 N_0 M_1 M_0}{N^2 (N-1)}}}$$

### Match-pairs

With matched-pairs, each case-control pair represents an observation. Matched pairs are then cross-tabulated like this:

	Control E+	Control E-
Case E+	$t$	$u$
Case E-	$v$	$w$

- The **odds ratio** is  $\hat{OR} = \frac{u}{v}$
- The standard error of natural log (ln) of the odds ratio is  $SE = \sqrt{\frac{1}{u} + \frac{1}{v}}$ , and the the 95% confidence interval for the *OR* parameter is given by  $e^{\ln \hat{OR} \pm (1.96)(SE)}$
- A *P* value can be derived with this test statistic 
$$z = \sqrt{\frac{(u-v)^2}{u+v}}$$