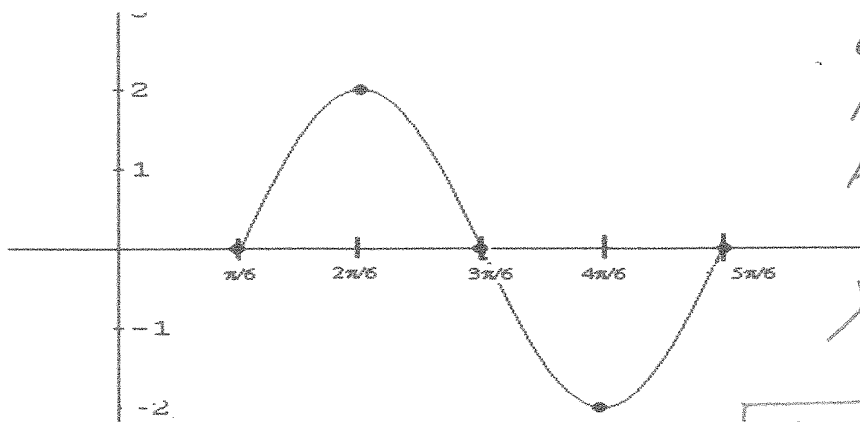


7. Find an equation of the form  $y = a \sin(bx - c) + d$  whose one cycle of the graph is shown below. (5 pts)



$$a = 2$$

$$\text{Period} = \frac{2\pi}{3} = \frac{2\pi}{b} \Rightarrow b = 3$$

$$\text{phase shift} = \frac{\pi}{6}$$

$$d = 0$$

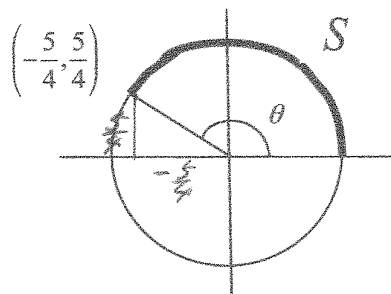
$$y = 2 \sin \left[ 3 \left( x - \frac{\pi}{6} \right) \right]$$

$$y = 2 \sin \left( 3x - \frac{\pi}{2} \right) + 0$$

8. Given that the point  $\left(-\frac{5}{4}, \frac{5}{4}\right)$  is a point on the terminal side of an angle  $\theta$ , consider the diagram below. (4 pts each)

- (a) Find the exact radius of the circle.

$$r = \sqrt{\left(-\frac{5}{4}\right)^2 + \left(\frac{5}{4}\right)^2} = \sqrt{\frac{25}{16} + \frac{25}{16}} = \sqrt{\frac{50}{16}} = \frac{5\sqrt{2}}{4}$$



- (a) Find the exact angle  $\theta$ .

$$\tan \theta = \frac{\frac{5}{4}}{-\frac{5}{4}} = -1 \Rightarrow \theta = \frac{3\pi}{4}$$

- (b) Find the exact value of  $\cot \theta$ .

$$\cot \theta = \cot \left( \frac{3\pi}{4} \right) = -1$$